

Nullable, First and Follow

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$E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \mathbf{id}$
 $F \rightarrow \mathbf{num}$
 $F \rightarrow (E)$

Esta é a gramática livre de contexto!

$E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

Acertando a gramática

Símbolo inicial: **E**

Novo símbolo inicial: **S**

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

Acertando a gramática

Símbolo inicial: **E**

Novo símbolo inicial: **S**

Nova regra de produção: $S \rightarrow E \$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow

Tabela de símbolos anuláveis, conjuntos first e conjuntos follow

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S			
E'			
T			
T'			
F			
E			

Tabela de símbolos anuláveis, conjuntos first e conjuntos follow

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×		
T	×		
T'	×		
F	×		
E	×		

Encontrando os símbolos não terminais anuláveis

Inicialmente nenhum símbolo não terminal é anulável

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
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 $E' \rightarrow - T E'$
 $E' \rightarrow$
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 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
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 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
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 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x		
T	x		
T'	x		
F	x		
E	x		

Regra com terminal no lado direito é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x ✓		
T	x		
T'	x		
F	x		
E	x		

Lado direito da regra é vazio

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x ✓		
T	x		
T'	x ✓		
F	x		
E	x		

Lado direito da regra é vazio

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x ✓		
T	x		
T'	x ✓		
F	x		
E	x		

Lado direito da regra não é anulável

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x ✓		
T	x		
T'	x ✓		
F	x		
E	x		

Lado direito da regra não é anulável

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	x		
E'	x ✓		
T	x		
T'	x ✓		
F	x		
E	x		

Encontrando os conjuntos first

Inicialmente são vazios

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow \epsilon$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow \epsilon$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

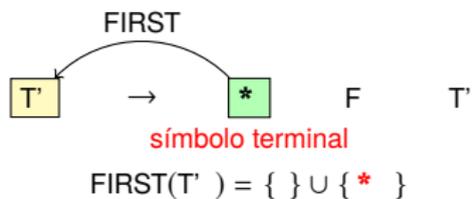
NT	Nullable	First	Follow
S	x		
E'	x ✓	+ -	
T	x		
T'	x ✓		
F	x		
E	x		

$E' \rightarrow$

O lado direito da regra é ϵ
Logo a regra é inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	× ✓	+ -	
T	×		
T'	× ✓	*	
F	×		
E	×		



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

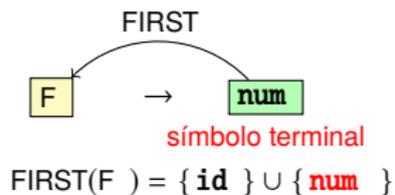
NT	Nullable	First	Follow
S	x		
E'	x ✓	+ -	
T	x		
T'	x ✓	* /	
F	x		
E	x		

$T' \rightarrow$

O lado direito da regra é ϵ
Logo a regra é inútil

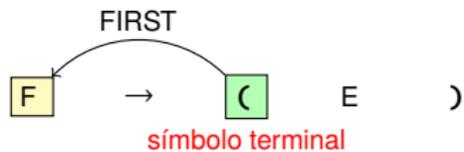
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×		
T'	×	* /	
F	×	id num	
E	×		



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

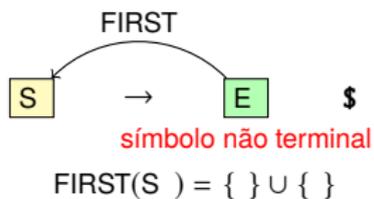
NT	Nullable	First	Follow
S	×		
E'	× ✓	+ -	
T	×		
T'	× ✓	* /	
F	×	id num (
E	×		



$$\text{FIRST}(F) = \{ id, num \} \cup \{ (\}$$

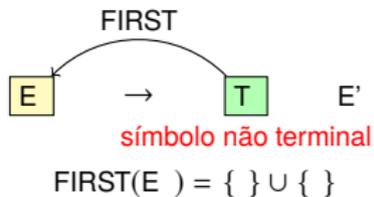
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×		
T'	×	* /	
F	×	id num (
E	×		



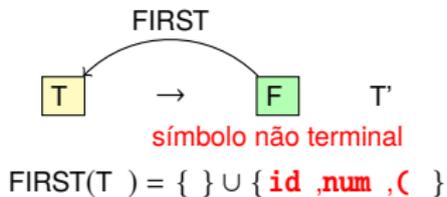
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×		
T'	×	* /	
F	×	id num (
E	×		



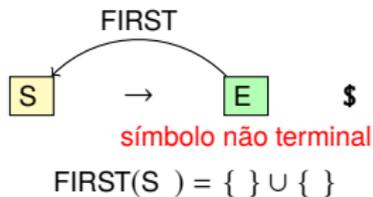
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×		



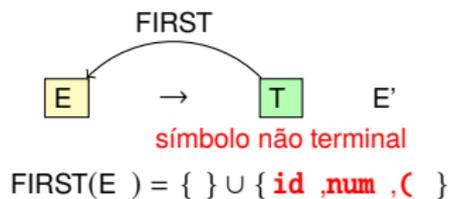
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×		



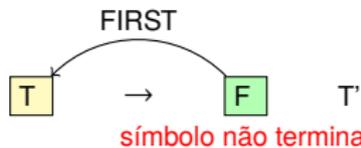
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

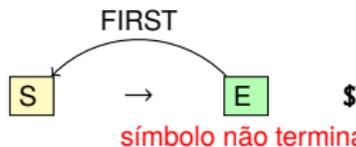
NT	Nullable	First	Follow
S	×		
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(T) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

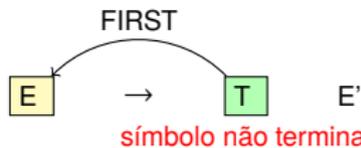
NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(S) = \{ \} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

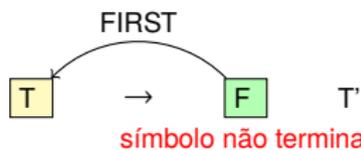
NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(E) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

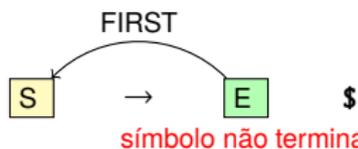
NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (
T'	× ✓	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(T) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

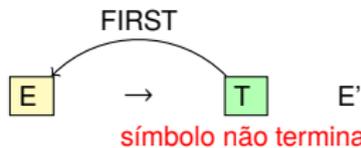
NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(S) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

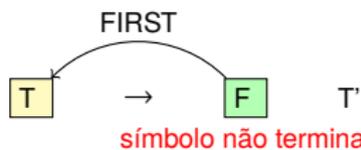
NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (
T'	×	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(E) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (
T'	× ✓	* /	
F	×	id num (
E	×	id num (



$$\text{FIRST}(T) = \{ id, num, (\} \cup \{ id, num, (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

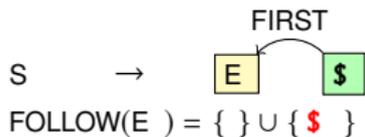
NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (
T'	× ✓	* /	
F	×	id num (
E	×	id num (

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (
T'	× ✓	* /	
F	×	id num (
E	×	id num (

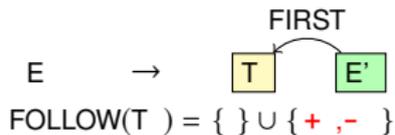
$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (
T'	× ✓	* /	
F	×	id num (
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

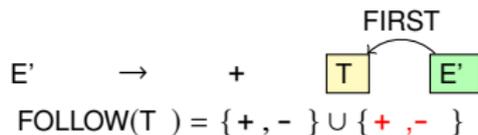
NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (
E	×	id num (\$

E → T E'

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (+ -
T'	×	* /	
F	×	id num (
E	×	id num (\$

$E' \rightarrow + T E'$

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (
E	×	id num (\$

$E' \rightarrow - T E'$

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (+ -
T'	×	* /	
F	×	id num (
E	×	id num (\$

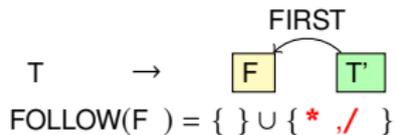
$E' \rightarrow$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

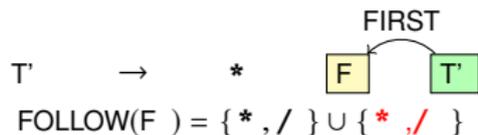
NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$

T → F T'

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

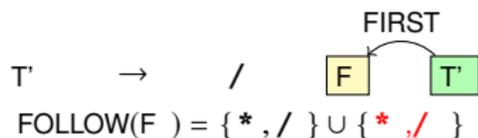
NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$

$T' \rightarrow * F T'$

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (+ -
T'	×	* /	
F	×	id num (* /
E	×	id num (\$

$T' \rightarrow / F T'$

Não há nenhum símbolo após o último não terminal

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	
T	×	id num (+ -
T'	×	* /	
F	×	id num (* /
E	×	id num (\$

$T' \rightarrow$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$

$F \rightarrow id$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$

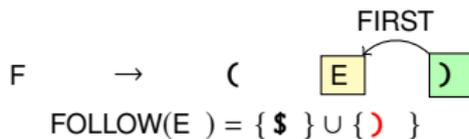
$F \rightarrow num$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

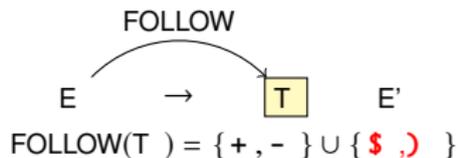
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 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	
T	×	id num (+ -
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$)



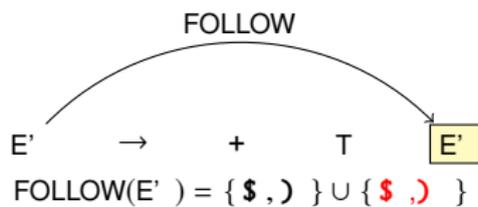
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 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
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 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	\$)
T	×	id num (+ - \$)
T'	×	* /	
F	×	id num (* /
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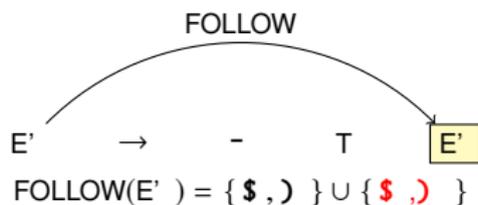
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 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
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NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$)



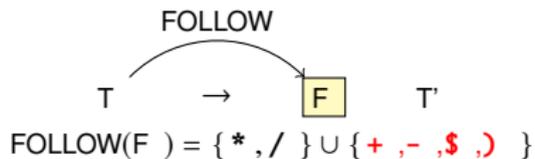
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 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
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 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	
F	×	id num (* /
E	×	id num (\$)



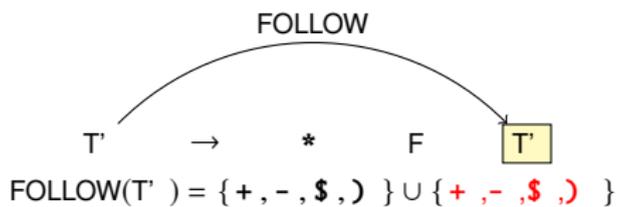
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 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
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 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



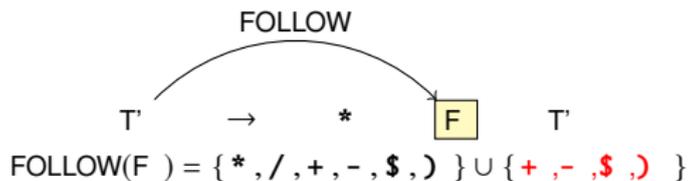
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 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
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 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



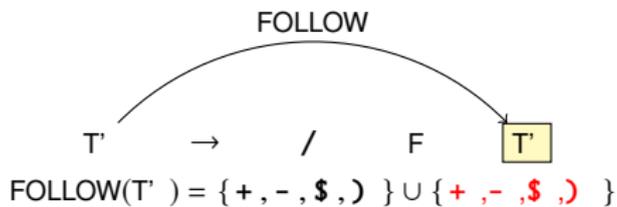
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 $T \rightarrow F T'$
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 $F \rightarrow num$
 $F \rightarrow (E)$

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S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



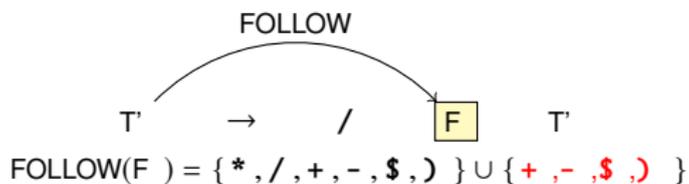
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 $E' \rightarrow$
 $T \rightarrow F T'$
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 $F \rightarrow num$
 $F \rightarrow (E)$

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S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
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E	×	id num (\$)



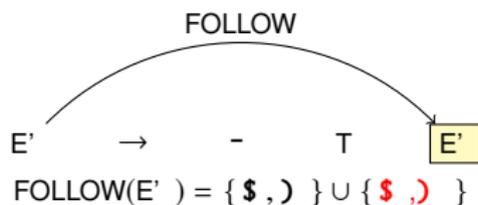
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 $T \rightarrow F T'$
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 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

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S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



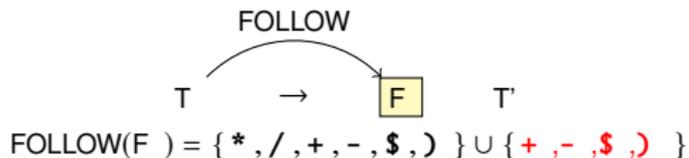
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S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
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F	×	id num (* / + - \$)
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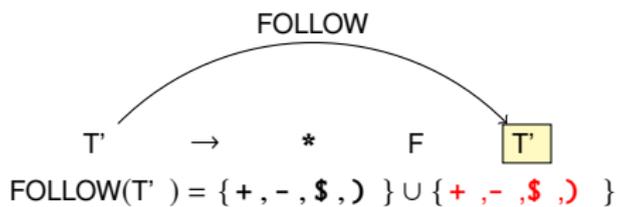
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S	×	id num (
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T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



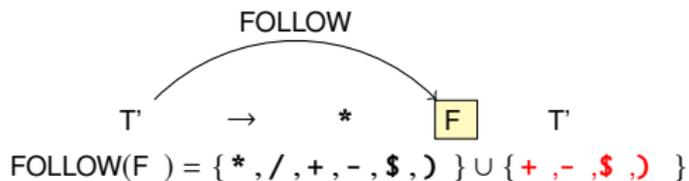
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S	×	id num (
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T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



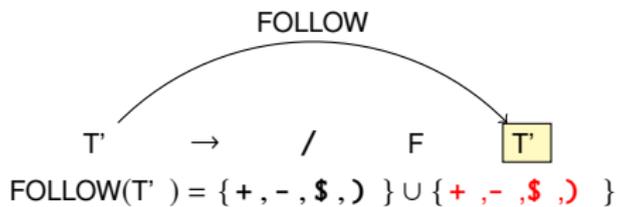
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S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



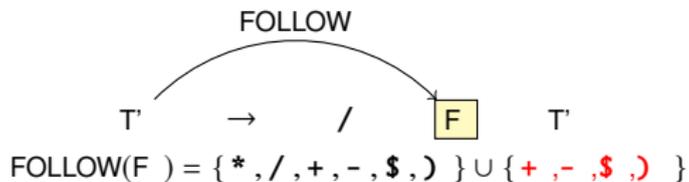
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 $T \rightarrow F T'$
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 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
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NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)



$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
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 $T \rightarrow F T'$
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 $F \rightarrow id$
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NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S									
E'									
T									
T'									
F									
E									

Construção da tabela LL(1)

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S									
E'									
T									
T'									
F									
E									

$$\text{FIRST}(E \$) = \{ \} \cup \{ id \text{ num } (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'									
T									
T'									
F									
E									

$S \rightarrow$ E $\$$
 $id \ num \ ($

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'									
T									
T'									
F									
E									

$$\text{FIRST}(T E') = \{ \} \cup \{ id \text{ num } (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'									
T									
T'									
F									
E		T E'						T E'	T E'

$E \rightarrow T E'$
 $id \ num \ ($

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'									
T									
T'									
F									
E		T E'						T E'	T E'

$$\text{FIRST}(+ T E') = \{ \} \cup \{ + \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'					+ T E'				
T									
T'									
F									
E		T E'						T E'	T E'

$E' \rightarrow + T E'$
 $+$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'					+ T E'				
T									
T'									
F									
E		T E'						T E'	T E'

$$\text{FIRST}(- T E') = \{ \} \cup \{ - \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'					+ T E'	- T E'			
T									
T'									
F									
E		T E'						T E'	T E'

$E' \rightarrow - T E'$
 -

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	€		€		+ T E'	- T E'			
T									
T'									
F									
E		T E'						T E'	T E'

$E' \rightarrow$
 $\$)$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow \epsilon$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow \epsilon$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T									
T'									
F									
E		T E'						T E'	T E'

$$\text{FIRST}(F T') = \{ \} \cup \{ id \text{ num } (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	€		€		+ T E'	- T E'			
T		F T'						F T'	F T'
T'									
F									
E		T E'						T E'	T E'

$T \rightarrow$ F T'
 id num (

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow \epsilon$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow \epsilon$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'									
F									
E		T E'						T E'	T E'

$$\text{FIRST}(* F T') = \{ \} \cup \{ * \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	€		€		+ T E'	- T E'			
T		F T'						F T'	F T'
T'				* F T'					
F									
E		T E'						T E'	T E'

$T' \rightarrow * F T'$
 $*$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'				* F T'					
F									
E		T E'						T E'	T E'

$$\text{FIRST}(/ F T') = \{ \} \cup \{ / \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	€		€		+ T E'	- T E'			
T		F T'						F T'	F T'
T'				* F T'			/ F T'		
F									
E		T E'						T E'	T E'

$T' \rightarrow / F T'$
 $/$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	€		€		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	€		€	* F T'	€	€	/ F T'		
F									
E		T E'						T E'	T E'

$T' \rightarrow$
 $+ - \$)$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F									
E		T E'						T E'	T E'

$$\text{FIRST}(id) = \{ \} \cup \{ id \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	\$)
T	×	id num (+ - \$)
T'	×	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F								id	
E		T E'						T E'	T E'

$F \rightarrow id$
 id

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F								id	
E		T E'						T E'	T E'

$$\text{FIRST}(num) = \{ \} \cup \{ num \}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	×	+ -	\$)
T	×	id num (+ - \$)
T'	×	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F								id	num
E		T E'						T E'	T E'

$F \rightarrow num$
 num

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow id$
 $F \rightarrow num$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F								id	num
E		T E'						T E'	T E'

$$\text{FIRST}((E)) = \{ \} \cup \{ (\}$$

$S \rightarrow E \$$
 $E \rightarrow T E'$
 $E' \rightarrow + T E'$
 $E' \rightarrow - T E'$
 $E' \rightarrow$
 $T \rightarrow F T'$
 $T' \rightarrow * F T'$
 $T' \rightarrow / F T'$
 $T' \rightarrow$
 $F \rightarrow \text{id}$
 $F \rightarrow \text{num}$
 $F \rightarrow (E)$

NT	Nullable	First	Follow
S	×	id num (
E'	× ✓	+ -	\$)
T	×	id num (+ - \$)
T'	× ✓	* /	+ - \$)
F	×	id num (* / + - \$)
E	×	id num (\$)

	\$	()	*	+	-	/	id	num
S		E \$						E \$	E \$
E'	ε		ε		+ T E'	- T E'			
T		F T'						F T'	F T'
T'	ε		ε	* F T'	ε	ε	/ F T'		
F		(E)						id	num
E		T E'						T E'	T E'

$F \rightarrow (E)$
 $($