

Nullable, First and Follow

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$S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

Esta é a gramática livre de contexto!

S → **if** E **then** S **else** S

S → **if** E **then** S

S → **cmd**

E → **id**

Acertando a gramática

Símbolo inicial: **S**

Novo símbolo inicial: **S'**

$S' \rightarrow S \$$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

Acertando a gramática

Símbolo inicial: S

Novo símbolo inicial: S'

Nova regra de produção: $S' \rightarrow S \$$

$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| | | | |
| | | | |
| | | | |

Tabela de símbolos anuláveis, conjuntos first e conjuntos follow

$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|-------|--------|
| S' | | | |
| S | | | |
| E | | | |

Tabela de símbolos anuláveis, conjuntos first e conjuntos follow

$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | × | | |
| S | × | | |
| E | × | | |

Encontrando os símbolos não terminais anuláveis

Inicialmente nenhum símbolo não terminal é anulável

$S' \rightarrow S$ \$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|-------|--------|
| S' | × | | |
| S | × | | |
| E | × | | |

Regra com terminal no lado direito é inútil

$S' \rightarrow S \ \$$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|-------|--------|
| S' | x | | |
| S | x | | |
| E | x | | |

Regra com terminal no lado direito é inútil

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | x | | |
| S | x | | |
| E | x | | |

Regra com terminal no lado direito é inútil

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | × | | |
| S | × | | |
| E | × | | |

Regra com terminal no lado direito é inútil

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | x | | |
| S | x | | |
| E | x | | |

Regra com terminal no lado direito é inútil

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
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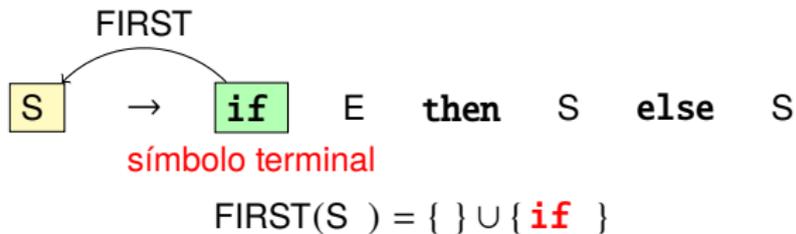
| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | × | | |
| S | × | | |
| E | × | | |

Encontrando os conjuntos first

Inicialmente são vazios

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|-------|--------|
| S' | × | | |
| S | × | if | |
| E | × | | |



$S' \rightarrow S \ \$$

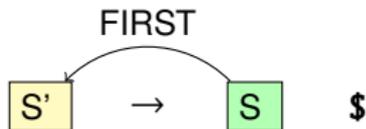
$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|----------------------|--------|
| S' | × | if cmd | |
| S | × | if cmd | |
| E | × | id | |



símbolo não terminal

$\text{FIRST}(S') = \{ \} \cup \{ \text{if}, \text{cmd} \}$

$S' \rightarrow S \ \$$

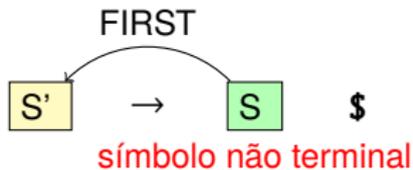
$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|----------------------|--------|
| S' | × | if cmd | |
| S | × | if cmd | |
| E | × | id | |



$$\text{FIRST}(S') = \{ \text{if}, \text{cmd} \} \cup \{ \text{if}, \text{cmd} \}$$

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|--------|
| S' | × | if cmd | |
| S | × | if cmd | |
| E | × | id | |

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|--------|
| S' | × | if cmd | |
| S | × | if cmd | |
| E | × | id | |

$S' \rightarrow S \ \$$

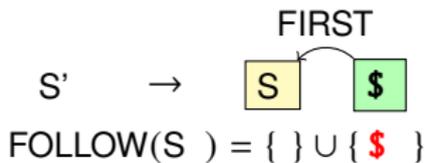
$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|--------|
| S' | × | if cmd | |
| S | × | if cmd | \$ |
| E | × | id | |



$S' \rightarrow S \ \$$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|--------|
| S' | × | if cmd | |
| S | × | if cmd | \$ |
| E | × | id | then |

FIRST

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$\text{FOLLOW}(E) = \{ \} \cup \{ \text{then} \}$

$S' \rightarrow S \ \$$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|-----------|
| S' | x | if cmd | |
| S | x | if cmd | $\$$ else |
| E | x | id | then |

$S \rightarrow \text{if } E \text{ then } \boxed{S} \overset{\text{FIRST}}{\curvearrowright} \boxed{\text{else}} S$

$\text{FOLLOW}(S) = \{ \$ \} \cup \{ \text{else} \}$

$S' \rightarrow S \ \$$

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

Não há nenhum símbolo após o último não terminal

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

$S \rightarrow \text{if } E \ \text{then } S$

FIRST

$\text{FOLLOW}(E) = \{ \text{then} \} \cup \{ \text{then} \}$

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

$S \rightarrow \text{if } E \text{ then } S$

Não há nenhum símbolo após o último não terminal

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

$S \rightarrow \text{cmd}$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

$E \rightarrow \text{id}$

Nenhum símbolo não terminal no lado direito da regra

Regra inútil

$S' \rightarrow S \ \$$

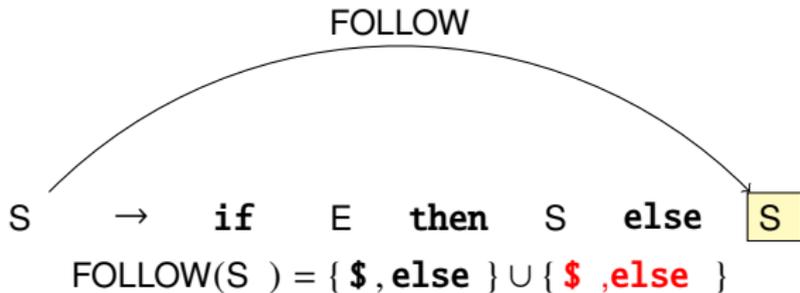
$S \rightarrow \text{if } E \text{ then } S \text{ else } S$

$S \rightarrow \text{if } E \text{ then } S$

$S \rightarrow \text{cmd}$

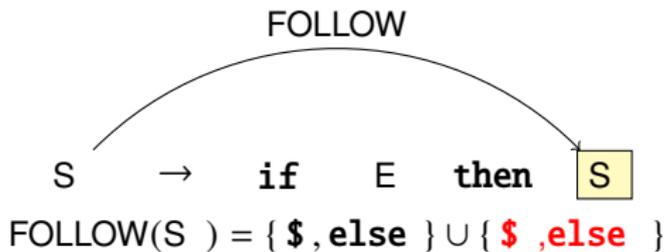
$E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|----------------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |



$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|----------------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |



$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|-----|------|----|----|------|
| S' | | | | | | |
| S | | | | | | |
| E | | | | | | |

Construção da tabela LL(1)

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|------|----|-----|------|----|----|------|
| S' | | | | | | |
| S | | | | | | |
| E | | | | | | |

$$\text{FIRST}(S \ \$) = \{ \} \cup \{ \text{if cmd} \}$$

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \ \text{then } S \ \text{else } S$
 $S \rightarrow \text{if } E \ \text{then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|------|------|----|------|------|
| S' | | S \$ | | | S \$ | |
| S | | | | | | |
| E | | | | | | |

$S' \rightarrow S \ \$$
 if cmd

$S' \rightarrow S \ \$$
 $S \rightarrow \mathbf{if} \ E \ \mathbf{then} \ S \ \mathbf{else} \ S$
 $S \rightarrow \mathbf{if} \ E \ \mathbf{then} \ S$
 $S \rightarrow \mathbf{cmd}$
 $E \rightarrow \mathbf{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|------|------|----|------|------|
| S' | | S \$ | | | S \$ | |
| S | | | | | | |
| E | | | | | | |

$$\text{FIRST}(\mathbf{if} \ E \ \mathbf{then} \ S \ \mathbf{else} \ S) = \{ \} \cup \{ \mathbf{if} \}$$

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \ \text{else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|-----------|
| S' | × | if cmd | |
| S | × | if cmd | $\$$ else |
| E | × | id | then |

| | $\$$ | cmd | else | id | if | then |
|------|------|----------|------|----|--------------------|------|
| S' | | $S \ \$$ | | | $S \ \$$ | |
| S | | | | | if E then S else S | |
| E | | | | | | |

$S \rightarrow \text{if } E \text{ then } S \ \text{else } S$
 if

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|------|----|----------|------|----|--------------------|------|
| S' | | $S \ \$$ | | | $S \ \$$ | |
| S | | | | | if E then S else S | |
| E | | | | | | |

$$\text{FIRST}(\text{if } E \text{ then } S) = \{ \} \cup \{ \text{if} \}$$

$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|------|------|----|-----------------------------------|------|
| S' | | S \$ | | | S \$ | |
| S | | | | | if E then S else S if E then S | |
| E | | | | | | |

$S \rightarrow \text{if } E \text{ then } S$
 if

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|------|----|----------|------|----|-----------------------------------|------|
| S' | | $S \ \$$ | | | $S \ \$$ | |
| S | | | | | if E then S else S if E then S | |
| E | | | | | | |

$$\text{FIRST}(\text{cmd}) = \{ \} \cup \{ \text{cmd} \}$$

$S' \rightarrow S \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|------|------|----|-----------------------------------|------|
| S' | | S \$ | | | S \$ | |
| S | | cmd | | | if E then S else S if E then S | |
| E | | | | | | |

$S \rightarrow \text{cmd}$
 cmd

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \ \text{else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|------|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|------|----|----------|------|----|-----------------------------------|------|
| S' | | $S \ \$$ | | | $S \ \$$ | |
| S | | cmd | | | if E then S else S if E then S | |
| E | | | | | | |

$$\text{FIRST}(\text{id}) = \{ \} \cup \{ \text{id} \}$$

$S' \rightarrow S \ \$$
 $S \rightarrow \text{if } E \text{ then } S \text{ else } S$
 $S \rightarrow \text{if } E \text{ then } S$
 $S \rightarrow \text{cmd}$
 $E \rightarrow \text{id}$

| NT | Nullable | First | Follow |
|----|----------|--------|---------|
| S' | × | if cmd | |
| S | × | if cmd | \$ else |
| E | × | id | then |

| | \$ | cmd | else | id | if | then |
|----|----|------|------|----|-----------------------------------|------|
| S' | | S \$ | | | S \$ | |
| S | | cmd | | | if E then S else S if E then S | |
| E | | | | id | | |

$E \rightarrow \text{id}$
 id